

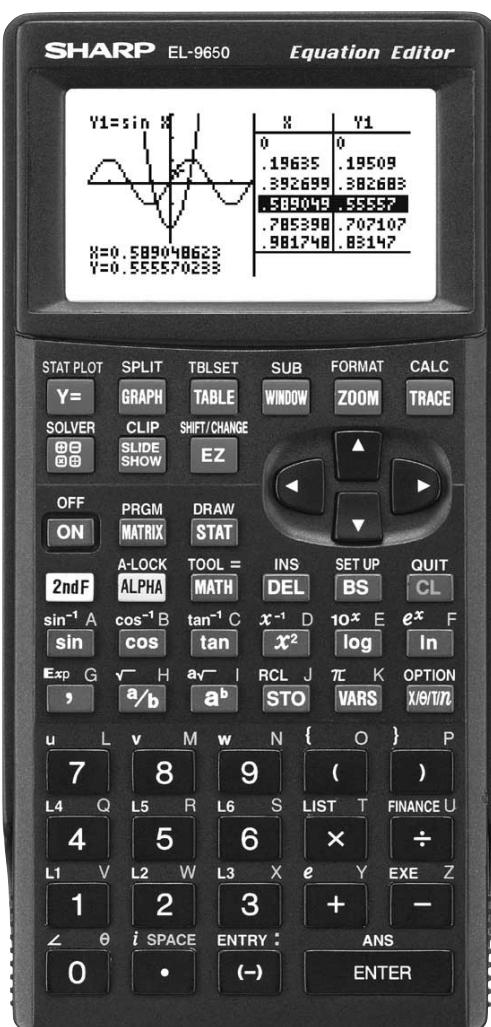
SHARP

Graphing Calculator

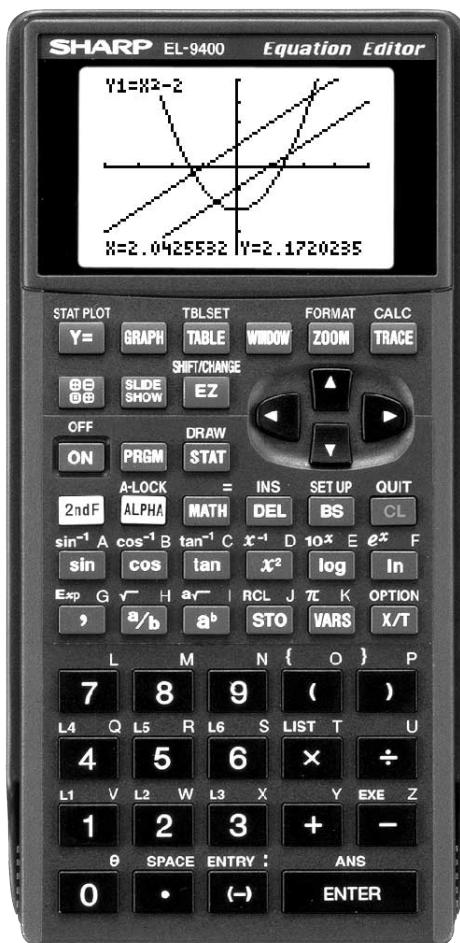
EL-9650/9400

Handbook Vol. 2

Programmes



EL-9650



EL-9400

Read this first

This handbook was produced for practical application of the SHARP EL-9650 and 9400 Graphing Calculator. Both calculators include a highly convenient programming function, which enables automatic processing of both simple and complex calculations any number of times.

We would like to express our deepest gratitude to all the teachers whose cooperation we received in editing this book. In order to produce a handbook which is more replete and useful to everyone, we would welcome any comments or ideas on exercises. If you wish to contribute to future editions, **use the attached blank sheet or contact us by e-mail : osksp@hsa.osa.sharp.co.jp (for Windows 95) or oskspm@hsb.osa.sharp.co.jp (for Macintosh)**. When sending the data by e-mail, please include relevant information such as the explanation of the programme, parameters used in the programme and the listing of the programme. Please note that the programmes you send us may be opened to the public at this home page site or in other Sharp publications.

Note: Certain problems can not be solved with the EL-9400 as indicated in contents.

1. Entering and Editing a Programme:

Programmes can be entered and edited either by pressing the calculator keys or by downloading from a PC. To download programmes from a PC, you will need the CE-LK1 PC link software (sold separately).

A. Using calculator keys

- Creating a new programme:

1. Press **2nd F PRGM** to display the programme menu.
2. Press **C ENTER** to select the new programme menu. (See right)
3. Enter the program title, then press **ENTER**.
4. Enter the programme.
5. Press **2nd F QUIT** to finish programming.



- Editing a programme:

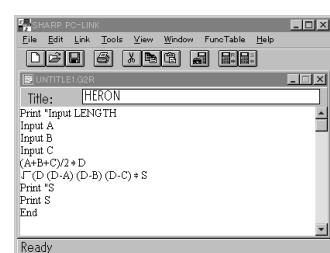
1. Press **2nd F PRGM** to display the programme menu.
2. Press **B** and choose the number of the programme you wish to edit. (See right)
3. Press **2nd F QUIT** to finish editing.



B. Downloading from PC

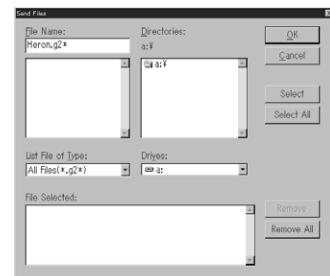
- Creating a new programme:

1. Using the CE-LK 1, select the **Model Type** from the **Tools** menu and click on the same model as your calculator.(click on EL-9600 for EL-9650)
2. Select **New** from the **File** menu.
3. Enter a programme name in **Title:**
4. Enter a program. (For details on entering a programme, refer to the operation manual.) (See right)



- Programmes can also be downloaded from Sharp's website at <http://www.sharp.co.jp/sc/excite/calculator/text/class96.htm> instead of creating a new programme.

- Sending programmes from a PC:
 1. Using the CE-LK1, select the **Communication Port** from the **Link** menu and click on the port to be used.
 2. Turn off the EL-9650/9400 and connect it to the PC.
 3. Turn on the EL-9650/9400
 4. Select **Send...** from the **Link** menu of the CE-LK1 (See right)
 5. Specify the kind of drive, folder, and file, then select the file to be sent from the file list, and click on the **Select** button.
 6. Click on the **OK** button.



Note: For further details refer to the manual.

2. Executing a programme:

1. Press **2nd F PRGM** to display the execute menu.
2. Press **A ENTER** and choose the number of the programme you wish to execute. (See right)
3. Follow the instructions.



3. Deleting a programme:

- Press **2nd F OPTION C** and then choose **5** to select the programme to be deleted.

No	1: L1	2: L2	3: L3
1	300	-----	-----
2	326		
3	323		
4	344		
5	300		
6	401		
7	300		

No	1: L1	2: L2	3: L3
4	344		
5	300		
6	401		
7	398		
8	450		
9	-----		

4. Using the keys:

- Press **2nd F** to use secondary functions (in yellow).
To select "sin⁻¹": **2nd F sin** → Displayed as follows: **2nd F sin⁻¹**

- Press **ALPHA** to use the alphabet keys (in blue).
To select A: **ALPHA sin** → Displayed as follows: **ALPHA A**

- Press **2nd F A-LOCK** to continue input of blue letters.
To input ABC: **ALPHA A ALPHA A ALPHA A** or **2nd F A-LOCK A A A**
(To return to the normal function, press **ALPHA** again.)

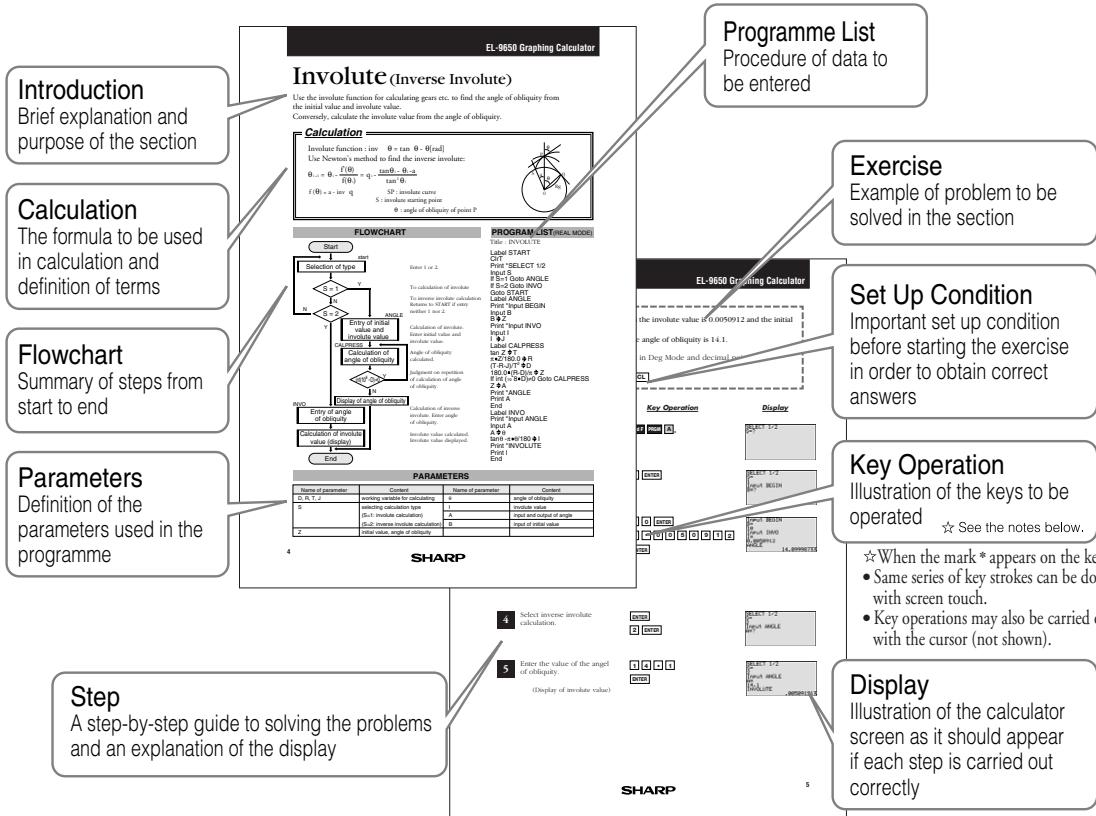
5. Troubleshooting:

Following is a list of error codes and error messages.

When errors occur, refer to pages 12, 254, or 27 of the manual.

Error code	Error message	Error content
01	Syntax	Syntax error in equation or programme
02	Calculate	Execution of a division using 0, calculation beyond calculation range, etc.
03	Nesting	Reservation of 14 or more numerical values or 32 or more functions during execution.
04	Invalid	Matrix definition error
05 for	Dimension	Inconsistency in the dimension of matrix during arithmetic of a matrix or dimension of list STAT calculation.
07	Invalid DIM	Size of list and matrix input for calculation exceeds calculation range.
08	Argument	Inconsistency in argument of the structured function
09	Data Type	Invalid data type used in calculation
11	No define	Undefined list or matrix
12	Domain	Argument definition outside of domain
13	Increment	Increment error
17	Stat Med	Med-Med law (statistic) error
20	No Argument	No argument entered
21	Not pair ∫ dx	Equation definition (∫ and dx as a pair) for integral calculus does not follow syntax.
22	Not pair []	Not paired with specified “[]”
23	Not pair ()	Not paired with specified “()”
24	Not pair { }	Not paired with specified “{ }”
32	No data	Data does not exist
33	Graph Type	Error in graph type setting
37	No title	No title entered
38	Too many obj	More than 30 objects selected
40	Lbl duplicate	Same label name is used more than once within a programme
41	Lbl undefined	Label is not defined for Goto or Gosub
42	Lbl over	More than 50 labels are used within a programme
43	Gosub stack	Nesting of more than 10 subroutine stacks
44	Line too long	One line of programme exceeds more than 160 characters
45	Can't return	Use of return command without jumping from subroutine
46	Strage full	Attempt to create a file exceeding 99 (delete unnecessary files)
47	Coord type	Invalid coordinate system for command
90	Memory over	Over memory capacity
99	System error	User memory space cannot be secured

6. Page Layout



Note: This handbook is only an example of how to use programming function of the EL-9650. The layout may vary with each screen.

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1. Heron's Formula	1
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*only for EL-9650

Other books available:

Graphing Calculator EL-9400 TEACHER'S GUIDE

Graphing Calculator EL-9650/9400 Handbook Vol. 1 (Algebra)

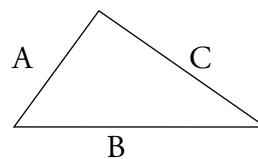
Heron's Formula

Use Heron's formula to find the area of a triangle when the sides (A,B,C) of the triangle are known.

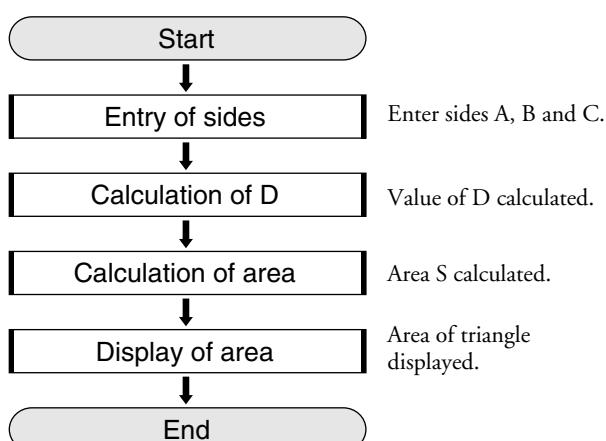
Calculation

$$S = \sqrt{D(D - A)(D - B)(D - C)}$$

$$D = \frac{(A + B + C)}{2}$$



FLOWCHART



PROGRAMME LIST (REAL MODE)

Title : HERON

```

Print "Input LENGTH
Input A
Input B
Input C
(A+B+C)/2⇒D
√(D(D-A)(D-B)(D-C))⇒S
Print "S =
Print S
End
  
```

PARAMETERS

Name of parameter	Content	Name of parameter	Content
A	value of side A	D	value of D
B	value of side B	S	area
C	value of side C		

Exercise

Find the area of a triangle when sides A, B and C are 20, 35 and 40cm respectively.

Step

Key Operation

Display

(When using EL-9650)

- 1 Specify the programme mode.
Select the title HERON.

2nd F **PRGM** **A***

HERON
INPUT LENGTH
A=?

- 2 Enter the values A, B and C.

2 **0** **ENTER** **3** **5**
ENTER **4** **0** **ENTER**

A=
20
B=
35
C=
40
S=
349.944192

(Display of area)

- 3 The area is approximately 350cm².

Calculating Tension

Use the law of sines to find the tension when a pole of weight W is suspended with two strings, and the strings are balanced with the angles from the vertical line A and B.

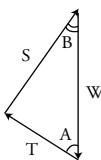
Calculation

$$\frac{T}{\sin B} = \frac{S}{\sin A} = \frac{W}{\sin (A+B)}$$

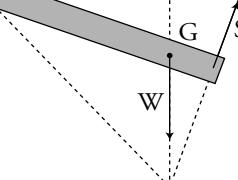
$$\therefore T = W \frac{\sin B}{\sin (A+B)}$$

$$\therefore S = W \frac{\sin A}{\sin (A+B)}$$

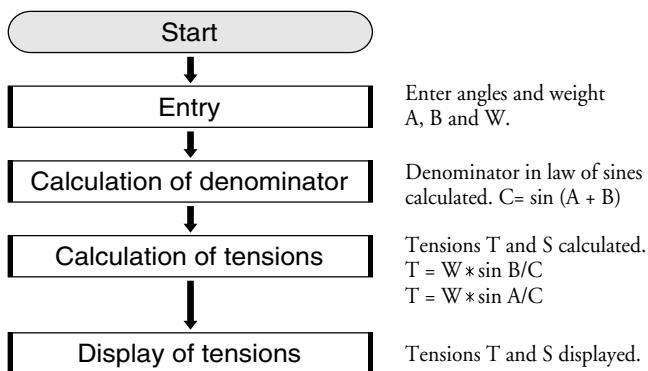
T, S : tension W : weight
A, B : angles (6 sexagesimal numbers)



vertical line



FLOWCHART



PROGRAMME LIST (REAL MODE)

Title : TENSION

```

Print "Input ANGLE
Input A
Input B
Print "Input WEIGHT
Input W
sin (A+B)⇒C
W*sin B/C⇒T
W*sin A/C⇒S
Print "TENSION
Print "T=
Print T
Print "S=
Print S
End

```

PARAMETERS

Name of parameter	Content	Name of parameter	Content
A	angle A	S	tension S
B	angle B	T	tension T
C	sin(A+B)	W	weight

Exercise

Calculate the tension assuming weight=40kg, angle A=30° 15' 20", and angle B=27° 45' 40". Enter the angles with sexagesimal numbers.

Set up condition: decimal point digit number in TAB 3 Mode, decimal point in Fix Mode, and angle unit in Deg Mode.

2nd F SET UP C * 2 * D * 3 * B * 1 * CL

Step**Key Operation****Display**

(When using EL-9650)

- 1** Specify the programme mode.
Select the title TENSION.

2nd F PRGM A *

TENSION
Input ANGLE
A=?

- 2** Enter the values of angles A and B.

3 0 • 1 5 2 0

ENTER

2 7 • 4 5 4 0

ENTER

Input ANGLE
A= 30.1520
B= 27.4540
Input WEIGHT
W=?

- 3** Enter the value of weight.

4 0 ENTER

Input WEIGHT
W= 40
TENSION
T= 21.840
S= 23.795

- 4** Tension T is 21.840kg and S is 23.795kg.

Involute (Inverse Involute)

Use the involute function for calculating gears etc. to find the angle of obliquity from the initial value and involute value.

Conversely, calculate the involute value from the angle of obliquity.

Calculation

Involute function : $\text{inv } \theta = \tan \theta - \theta [\text{rad}]$

Use Newton's method to find the inverse involute:

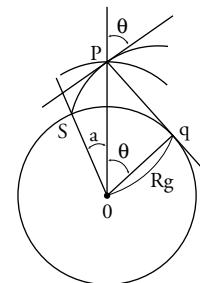
$$\theta_{i+1} = \theta_i - \frac{f(\theta)}{f'(\theta)} = \theta_i - \frac{\tan \theta_i - \theta_i - a}{\tan^2 \theta_i}$$

$$f(\theta) = a - \text{inv } \theta$$

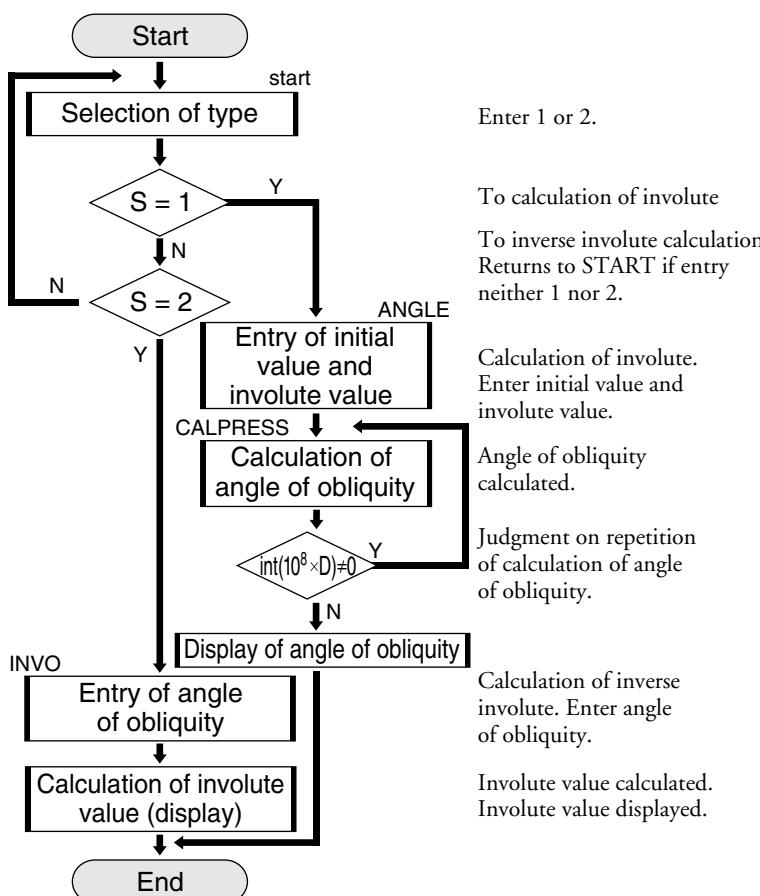
SP : involute curve

S : involute starting point

θ : angle of obliquity of point P



FLOWCHART



PROGRAMME LIST (REAL MODE)

```

Title : INVOLUTE
Label START
ClrT
Print "SELECT 1/2"
Input S
If S=1 Goto ANGLE
If S=2 Goto INVO
Goto START
Label ANGLE
Print "Input BEGIN"
Input B
B → Z
Print "Input INVO"
Input I
I → J
Label CALPRESS
tan Z → T
π*Z/180.0 → R
(T-R-J)/T² → D
180.0*(R-D)/π → Z
If int (10^8*D)≠0 Goto CALPRESS
Z → A
Print "ANGLE"
Print A
End
Label INVO
Print "Input ANGLE"
Input A
A → θ
tanθ -π*θ/180 → I
Print "INVOLUTE"
Print I
End

```

PARAMETERS

Name of parameter	Content	Name of parameter	Content
D, R, T, J	working variable for calculating	θ	angle of obliquity
S	selecting calculation type (S=1: involute calculation) (S=2: inverse involute calculation)	I	involute value
Z	initial value, angle of obliquity	A	input and output of angle
		B	input of initial value

Exercise

- (1) Find the angle of obliquity when the involute value is 0.0050912 and the initial value is 10.
 (2) Find the involute value when the angle of obliquity is 14.1.

Set up condition: angle unit in Deg Mode and decimal point in Float Pt Mode.

2nd F SET UP B * 1 * C * 1 * CL

Step**Key Operation****Display**
(When using EL-9650)

- 1** Specify the programme mode.
 Select the title INVOLUTE.

2nd F PRGM A *

SELECT 1/2
S=?

- 2** Select involute calculation.

1 ENTER

SELECT 1/2
S=?
1
Input BEGIN
B=?

- 3** Enter the initial value and the involute value.

1 0 ENTER

**0 • 0 0 5 0 9 1 2
ENTER**

Input BEGIN
B=
10
Input INVO
I=
0.0050912
ANGLE
14.09998733

(Display of angle of obliquity)

- 4** Select inverse involute calculation.

ENTER

2 ENTER

SELECT 1/2
S=?
2
Input ANGLE
A=?

- 5** Enter the value of the angle of obliquity.

1 4 • 1

ENTER

(Display of involute value)

SELECT 1/2
S=?
2
Input ANGLE
A=
14.1
INVOLUTE
.005091213

Calculating Illuminance and Luminous Intensity

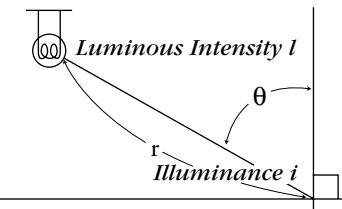
Enter the luminous intensity of luminous source, distance, the angle between the perpendicular line and light ray, to find the illuminance of the illuminated side.

Conversely, find the luminous intensity of the source from the illuminance of the illuminated side.

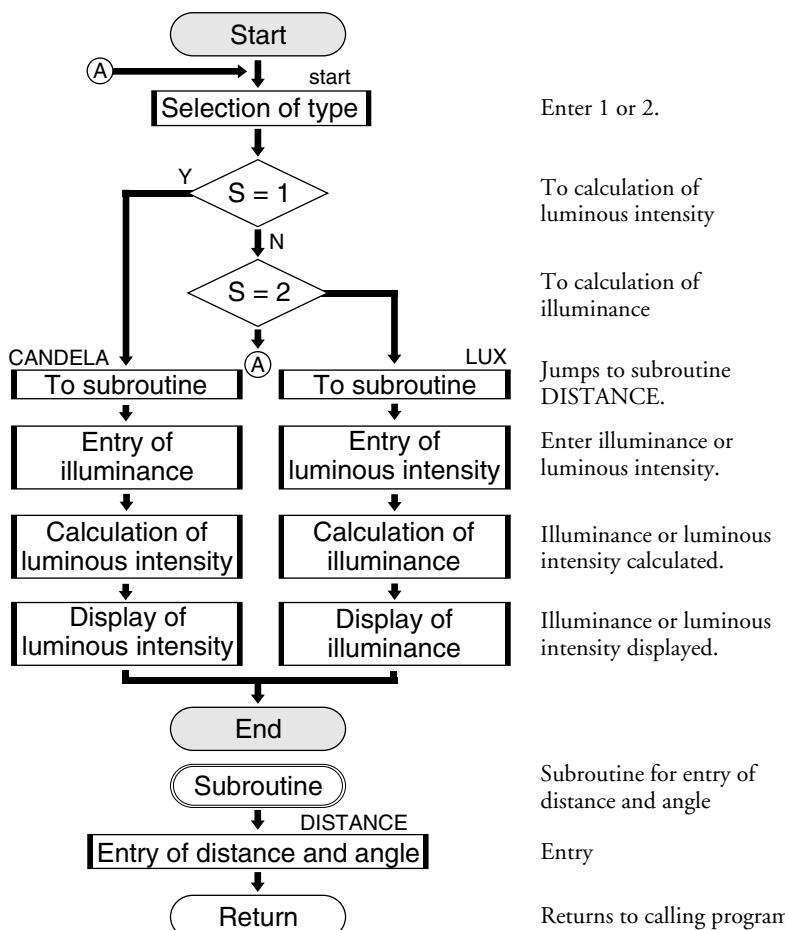
Calculation

$$i = \frac{l \cdot \cos \theta}{r^2} \quad l = \frac{r^2 \cdot i}{\cos \theta}$$

i : illuminance [lux]
 r : distance [m]
 θ : angle [$^\circ$]



FLOWCHART



PROGRAM LIST (REAL MODE)

```

Title : CAND LUX
Label START
ClrT
Print "CANDELA=1 LUX=2
Print "SELECT 1/2
Input S
If S=1 Goto CANDELA
If S=2 Goto LUX
Goto START
Label CANDELA
Gosub DISTANCE
Print "Input LUX
Input L
L → I
R²*I/cos θ → C
Print "CANDELA
Print C
End
Label LUX
Gosub DISTANCE
Print "Input CANDELA
Input C
C → K
K*cos θ /R² → L
Print "LUX
Print L
End
Label DISTANCE
Print "Input DISTANCE
Input D
D → R
Print "Input ANGLE
Input A
A → θ
Return

```

PARAMETERS

Name of parameter	Content	Name of parameter	Content
I	illuminance of illuminated side	θ	angle
K	luminous intensity of luminous source	A	input of angle
R	distance	L	input and calculating luminous intensity
S	selecting calculation type (S=1: calculation of luminous intensity) (S=2: calculation of illuminance)	D	input of distance
		C	input and calculating illuminance

Exercise

- (1) Find the luminous intensity of the luminous source of distance 10m, angle 60° and illuminance 20 lux.
 (2) Find the illuminance of the illuminated side of distance 10m, angle 60° and luminous intensity 4000 candela.

Set up condition: angle unit in Deg Mode and decimal point in
Float Pt Mode.

2nd F SET UP B.* 1.* C.* 1.* CL

Step**Key Operation****Display**

(When using EL-9650)

- 1** Specify the programme mode.
Select the title CAND LUX.

2nd F PRGM A.*

CANDELA=1 LUX=2
SELECT 1/2
S=?

- 2** Select calculation of luminous
intensity.

1 ENTER

CANDELA=1 LUX=2
SELECT 1/2
S=
1
Input DISTANCE
D=?

- 3** Enter the values of distance,
angle, and illuminance.

1 0 ENTER 6 0 ENTER
2 0 ENTER

(Display of luminous intensity)

SELECT 1/2
S=
1
Input DISTANCE
D=
10
Input ANGLE
A=
60
Input LUX
L=
20
CANDELA
4000

- 4** Select calculation of illuminance.
Enter the values of distance,
angle, and luminous intensity.

ENTER 2 ENTER
1 0 ENTER
6 0 ENTER
4 0 0 0 ENTER

(Display of illuminance)

Input ANGLE
A=
60
Input CANDELA
C=
4000
LUX
20

Calculating Simple Harmonic Oscillation

Enter period, amplitude and time to calculate displacement at specified time, acceleration, angular velocity, and velocity. Also, display the changes during the entered time period on a graph.

Calculation

$$\text{angular velocity : } \omega = \frac{2\pi}{T}$$

$$\text{acceleration : } a = -\omega^2 x$$

A : amplitude

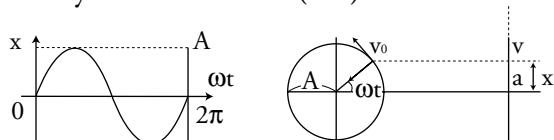
t : time [sec]

T : period [sec]

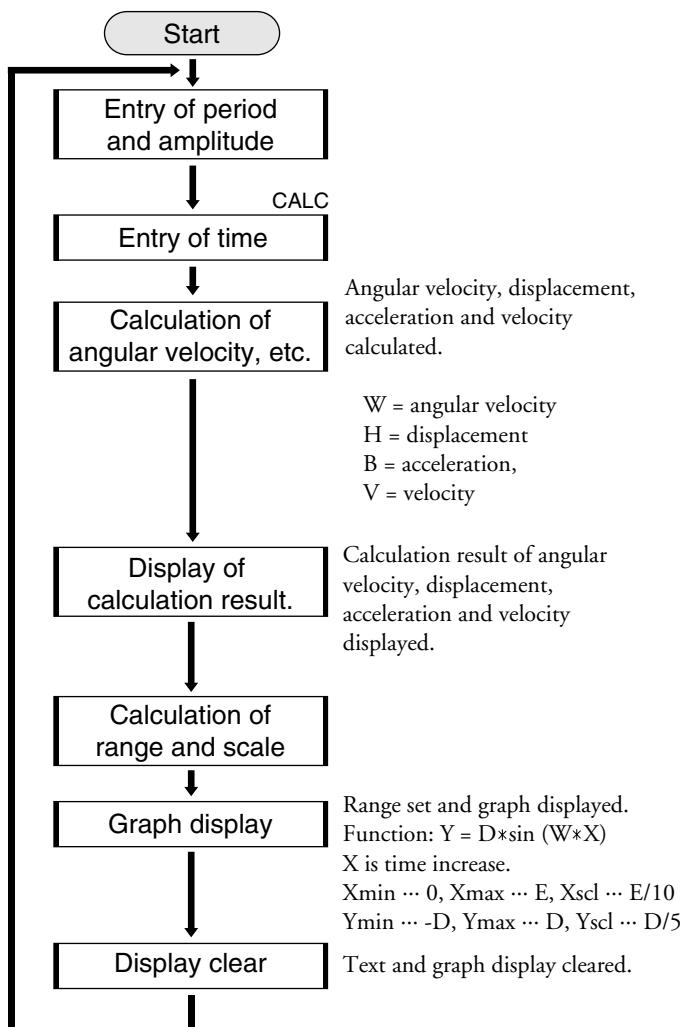
ω : angular velocity [rad/sec]

$$\text{displacement : } x = A \times \sin(\omega t)$$

$$\text{velocity : } v = A \times \omega \times \cos(\omega t)$$



FLOWCHART



PROGRAMME LIST (REAL MODE)

Title : OSCILLAT

```

Print "Input PERIOD
Input P
P⇒F
Print "Input AMPLITUDE
Input A
A⇒D
Label CALC
Print "Input TIME
Input T
T⇒E
2*π/F⇒W
D*sin (W*E)⇒H
-(W^2)*H⇒B
D*W*cos (W*E)⇒V
Print "ANGULAR VELOCITY
Print W
Print "MAGNITUDE
Print H
Print "ACCELERATION
Print B
Print "VELOCITY
Print V
Wait
E/10⇒X scl
D/5⇒Y scl
0⇒Xmin:E⇒Xmax
-D⇒Ymin:D⇒Ymax
Draw D*sin (W*X)
Wait
ClrT
ClrG
Goto CALC

```

PARAMETERS

Name of parameter	Content	Name of parameter	Content
B	acceleration	A	input of amplitude
E	time	P	input of period
V	velocity	T	input of time
W	angle of velocity (ω)	D	amplitude
H	displacement	F	period
Xscl	x-axis scale	X	time increase
Yscl	y-axis scale		

Exercise

Calculate angular velocity, etc., using period π , amplitude 1 and time 3 seconds and display the changes on a graph.

Set up condition: angle unit in Rad Mode and decimal point in Float Pt Mode.

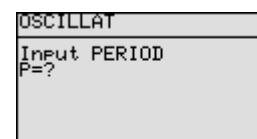
2nd F SET UP B * 2 * C * 1 * CL

Step**Key Operation****Display**

(When using EL-9650)

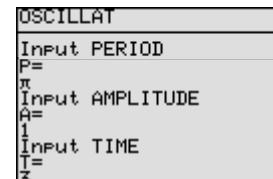
- 1** Specify the programme mode.
Select the title OSCILLAT.

2nd F PRGM A *



- 2** Enter the values of period, amplitude, and time.

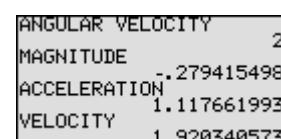
2nd F π ENTER 1 ENTER 3



- 3**

ENTER

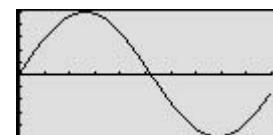
(Display of angular velocity)
(Display of displacement)
(Display of acceleration)
(Display of velocity)



- 4**

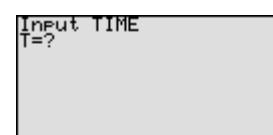
ENTER

(Display of graph of simple harmonic oscillation)



- 5**

ENTER



Electric Power Consumed on an AC Circuit

Enter the voltage effective value, frequency and resistance value to find the power value of the circuit with resistance R. Draw a graph of the changes in power over a period of time.

Calculation

P : power consumption I : effective value of current

V : effective value of voltage

$$I_0 = N \cdot \sin \omega \cdot t \quad V_0 = M \cdot \sin \omega \cdot t \quad P_0 = I_0 \cdot V_0$$

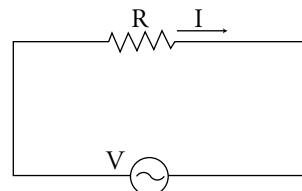
P_0 : change in amount of power with time

I_0 : change in amount of current with time

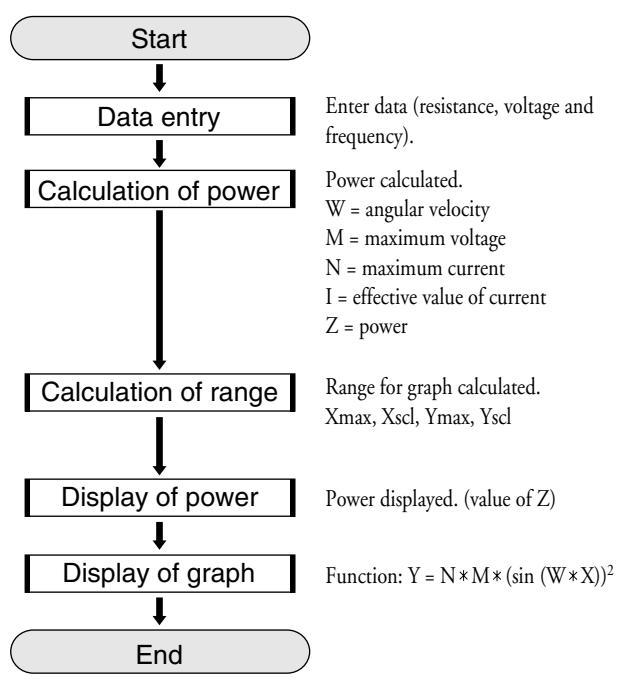
V_0 : change in amount of voltage with time

N: maximum value of current M: maximum value of voltage

ω : angular velocity ($2\pi S$) t : time S : frequency



FLOWCHART



PROGRAM LIST (REAL MODE)

Title : AC POWER
Print "Input RESISTANCE
Input R
Print "Input VOLTAGE
Input V
Print "Input FREQUENCY
Input F
R⇒T
V⇒D
F⇒S
 $2*\pi*S \Rightarrow W$
 $D*\sqrt{2} \Rightarrow M$
M/T⇒N
 $N/\sqrt{2} \Rightarrow I$
D*I⇒Z
1/S⇒Xmax
Xmax/10⇒Xscl
N*M⇒Ymax
Ymax/10⇒Yscl
Print "WATT=
Print Z
Wait
0⇒Xmin
0⇒Ymin
Draw $N*M*(\sin(W*X))^2$
End

PARAMETERS

Name of parameter	Content	Name of parameter	Content
S	frequency	Xscl	scale of x-axis
I	effective value of current	Ymax	maximum value of y-axis
T	resistance value	Yscl	scale of y-axis
D	effective value of voltage	V	input of voltage
W	angular velocity	R	input of resistance value
N	maximum value of current	F	input of frequency
M	maximum value of voltage	Z	value of power
Xmax	maximum value of x-axis		

Exercise

Find the power value of an AC circuit with resistance value 150Ω , voltage effective value 100V and frequency 50Hz and display on a graph the changes in power over a period of time.

Set up condition: angle unit in Rad Mode and decimal point in Float Pt Mode.

2nd F SET UP B.* 2.* C.* 1.* CL

Step**Key Operation****Display**

(When using EL-9650)

- 1** Specify the programme mode.
Select the title AC POWER.

2nd F PRGM A.*

AC POWER
Input RESISTANCE
R=?

- 2** Enter the resistance value, voltage effective value, and frequency.

1 5 0 ENTER
1 0 0 ENTER
5 0 ENTER

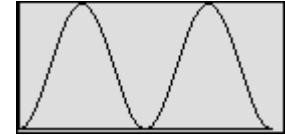
Input RESISTANCE
R= 150
Input VOLTAGE
V= 100
Input FREQUENCY
F= 50
WATT= 66.66666667

(Display of value power)

- 3**

ENTER

(Display of graph)



Angle of Vector

Use the matrix operation feature to find the angle θ which forms the standard vector and vector. The angle can be calculated at one time against the multiple vectors.

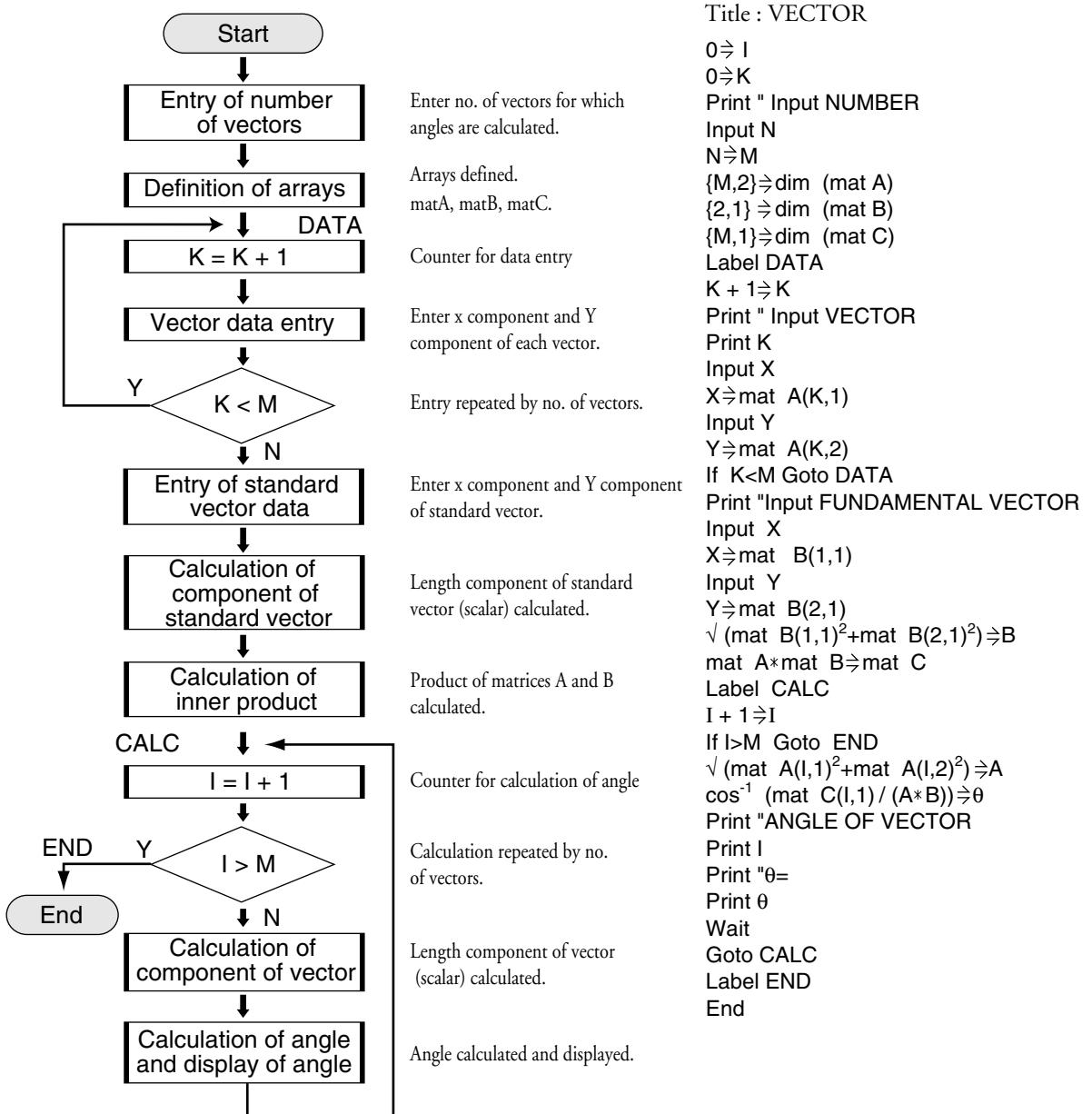
Calculation

Calculating vector inner product $\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta$

Use the above expression to derive the following expression

$$\theta = \cos^{-1} \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| |\vec{b}|}$$

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PARAMETERS

Name of parameter	Content	Name of parameter	Content
A	vector scalar quantity	θ	vector angle
B	standard vector scalar quantity	K	display
I	calculating counter	N	input of number of vectors
K	input counter	mat A	vector components
M	number of vectors	mat B	standard vector components
X	input of x component	mat C	vector inner product
Y	input of y component		

Exercise

Calculate the angle formed by the following 3 vectors and standard vector (2,3).

vector 1 (5, 8)

vector 2 (7, 4)

vector 3 (9, 2)

Set up condition: angle unit in Deg mode, and decimal point in Float Pt mode.

2nd F SET UP B * 1 * C * 1 * CL

Step**Key Operation****Display**

- 1** Specify the programme mode.
Select the title VECTOR.

2nd F PRGM A*

VECTOR
Input NUMBER
N=?

- 2** Enter the number of vectors.

3 ENTER

VECTOR
Input NUMBER
N= 3
Input VECTOR
X=? 1

- 3** Enter the values of vector 1.

5 ENTER 8 ENTER

X= 5
Y= 8
Input VECTOR
X=? 2

- 4** Enter the values of vectors 2 and 3.

**7 ENTER 4 ENTER
9 ENTER 2 ENTER**

X= 9
Y= 2
Input FUNDAMENTAL VECT
OR X=? 3

- 5** Enter the value of standard vector.

2 ENTER 3 ENTER

X= 2
Y= 3
ANGLE OF VECTOR
θ= 1 1.684684318

(Display of angle of vector 1)

- 6** (Display of angle of vector 2)

ENTER

ANGLE OF VECTOR
θ= 2 26.56505118
ANGLE OF VECTOR
θ= 3 43.78112476

(Display of angle of vector 3)

ENTER

Linear Transformation

Use the matrix to find four types of the linear transformation of x-axis symmetric transformation, y-axis symmetric transformation, similar transformation and revolution around the origin.

Calculation

- Symmetric transformation to x-axis (Case 1)

$$\begin{pmatrix} X' \\ Y' \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$

- Symmetric transformation to y-axis (Case 2)

$$\begin{pmatrix} X' \\ Y' \end{pmatrix} = \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$

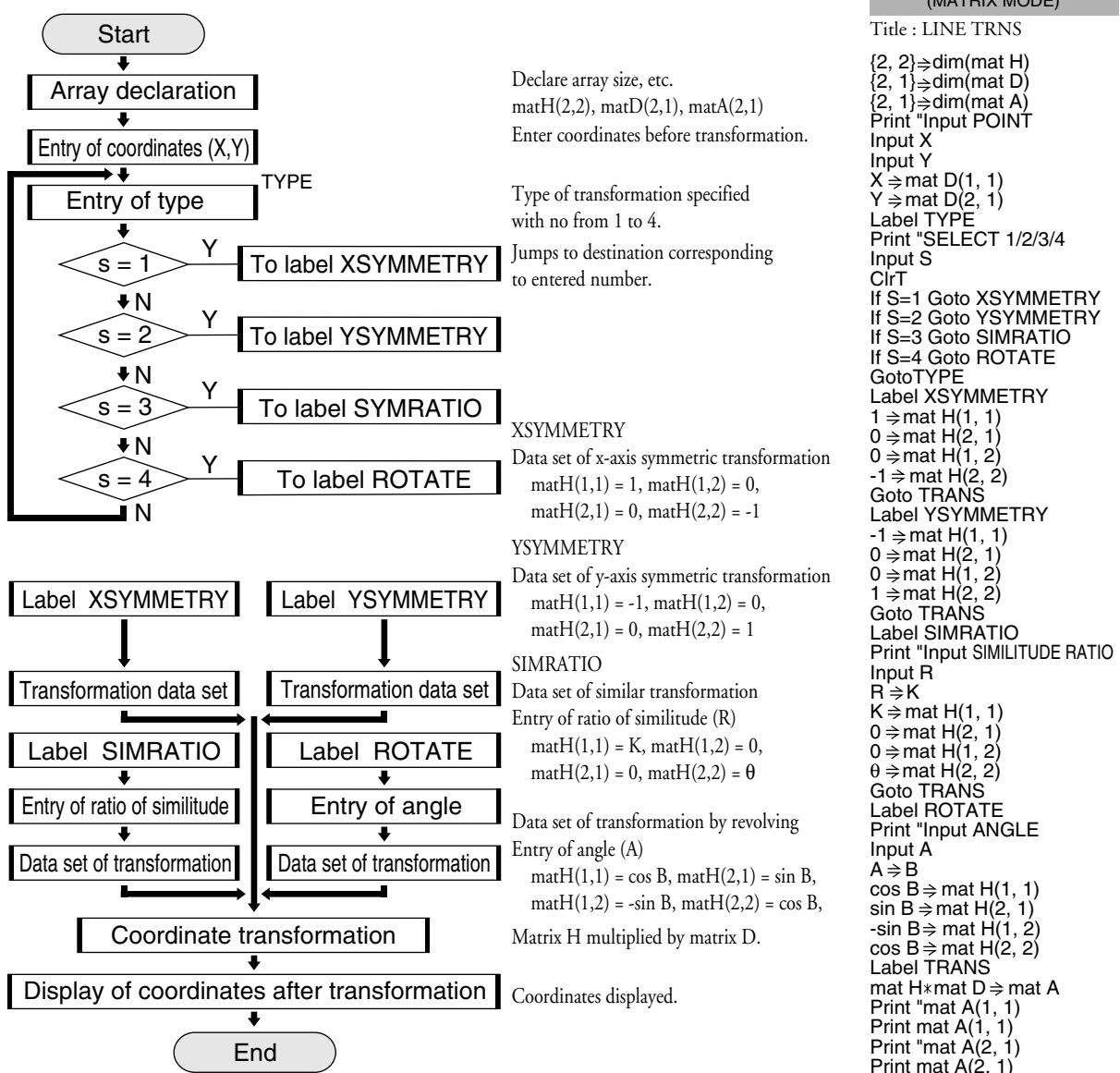
- Similar transformation with ratio of similitude K around origin (Case 3)

$$\begin{pmatrix} X' \\ Y' \end{pmatrix} = \begin{pmatrix} K & 0 \\ 0 & K \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$

- Transformation revolving around only angle B at the origin (Case 4)

$$\begin{pmatrix} X' \\ Y' \end{pmatrix} = \begin{pmatrix} \cos B & -\sin B \\ \sin B & \cos B \end{pmatrix} \begin{pmatrix} X \\ Y \end{pmatrix}$$

FLOWCHART



PARAMETERS

Name of parameter	Content	Name of parameter	Content
B	angle	Y	y-coordinate
K	ratio of similitude	A	input of angle
S	selecting type (S=1: case 1, S=2: case 2, S=3: case 3, S=4: case 4)	R	input of ratio of similitude
	mat A	mat H	coordinate after transformation
	mat D		transformation data
X	x-coordinate		x,y-coordinate

Exercise

1. Transform symmetrically the point (3, 5) to the x-axis.
2. Rotate the point (2, 6) at 45° around the origin.

Set up condition: angle unit in Deg Mode and decimal point in Float Pt Mode.

2nd F **SET UP** **B*** **1*** **C*** **1*** **CL**

Step	Key Operation	Display
1 Specify the programme mode. Select the title LINE TRNS.	2nd F PRGM A *	LINE TRN Input POINT X=?
2 Enter the values of the point.	3 ENTER 5 ENTER	Input POINT X= 3 Y= 5 SELECT 1/2/3/4 S=?
3 Select symmetric transformation to x-axis (case 1).	1 ENTER	mat A(1,1) mat A(2,1) 3 -5
.....		
4 Select transformation revolving around only angle B at the origin (case 4).	ENTER 2 ENTER 6 ENTER 4 ENTER	Input POINT X= 2 Y= 6 SELECT 1/2/3/4 S= 4
5 Enter the angle value.	4 5 ENTER	Input ANGLE A= 45 mat A(1,1) -2.828427125 mat A(2,1) 5.656854249

Moving Average

Plot a moving average graph which helps to understand how the results change over a specified period. The progress of sales and amounts of consumption and production can also be seen.

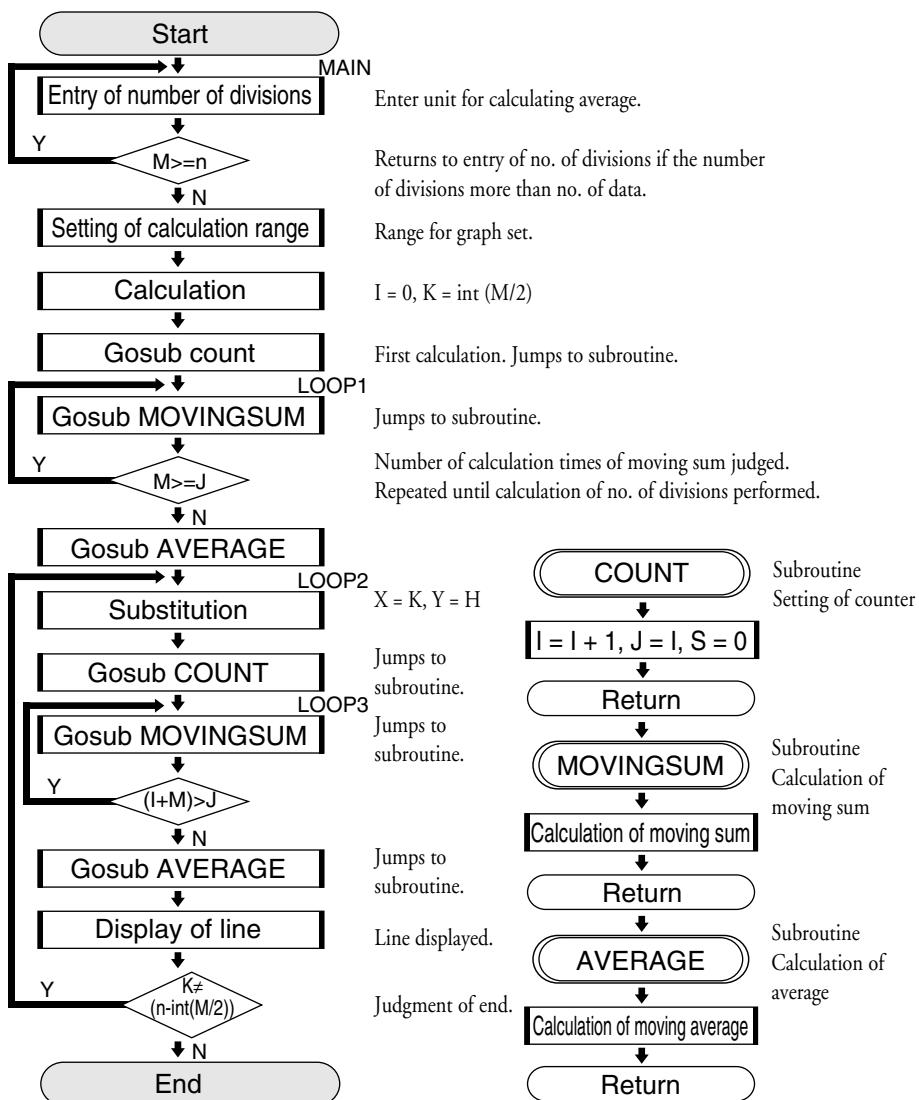
Calculation

$$H_i = \frac{X_{i-(M-1)/2} + \dots + X_i + \dots + X_{i+(M-1)/2}}{M}$$

$$(I = 1 + \frac{M-1}{2}, 2 + \frac{M-1}{2}, \dots, n + \frac{M-1}{2})$$

H_i : moving average
 M : number of divisions
 X_i : data
 n : number of data

FLOWCHART



PROGRAMME LIST (STAT MODE)

```
Title : MVIN AVG
Label MAIN
Print "Input DIVISION
Input D
D⇒M
1_Stats L1
If M≥n Goto MAIN
Rem RANGE
(xmax-xmin)/10⇒Yscl
0⇒Xmin
n⇒Xmax
1⇒Xscl
xmin⇒Ymin
xmax⇒Ymax
0⇒I
int (M/2)⇒K
Gosub COUNT
Label LOOP1
Gosub MOVINGSUM
If M≥J Goto LOOP1
Gosub AVERAGE
Label LOOP2
K⇒X
H⇒Y
Gosub COUNT
Label LOOP3
Gosub MOVINGSUM
If (I+M)>J Goto LOOP3
Gosub AVERAGE
Line (X, Y, K, H)
If K≠(n-int (M/2))Goto LOOP2
Wait
End
Label COUNT
I+1⇒I
I⇒J
0⇒S
Return
Label MOVINGSUM
S+L1(J)⇒S
J+1⇒J
Return
Label AVERAGE
S/M⇒H
K+1⇒K
Return
```

Parameters

name of parameter	content	name of parameter	content
H	moving average	S	moving sum
I	counter	X	starting point (x)
J	counter	Y	starting point (y)
K	counter	Yscl	scale of y-axis
M	number of divisions	B	input of number of divisions

Exercise

Find the moving average every three months (number of divisions: 3) from the following table of monthly sales.

Month	Jan.	Feb.	Mar.	Apr.	May.	Jun.	Jul.	Aug.
Sales[\$]	300	326	323	344	300	401	398	450

On the graph, Xmax = 8, Ymin = 300, and Ymax = 450.

Set up condition: decimal point in Float Pt Mode.

2nd F SET UP C * 1 * CL

Step**Key Operation****Display**

(When using EL-9650)

1

Enter statistical data into L1.

STAT A * ENTER

No	1: L1	2: L2	3: L3
1	300		
2	326		
3	323		
4	344		
5	300		
6	401		
7	398		
8	450		
9			

**3 0 0 ENTER 3 2 6
ENTER 3 2 3 ENTER
3 4 4 ENTER 3 0 0
ENTER 4 0 1 ENTER
3 9 8 ENTER 4 5 0
ENTER**

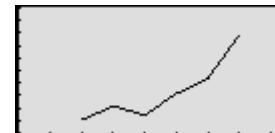
No	1: L1	2: L2	3: L3
1	300		
2	326		
3	323		
4	344		
5	300		
6	401		
7	398		
8	450		
9			

2Specify the programme mode.
Select the title MVIN AVG.**2nd F PRGM A ***

EXEC	01OSCILLAT
EDIT	02MVIN AVG
CNEW	03XY GRAPH
	04RUNGE
	05VARIANCE

3

Enter the number of divisions(3).

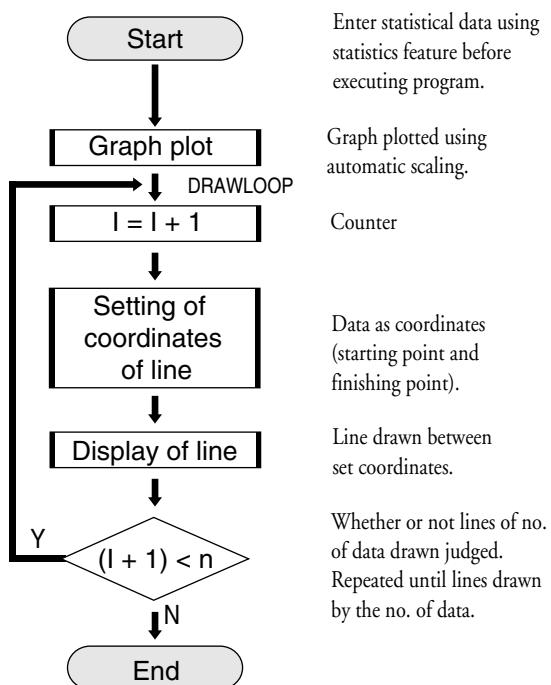
3 ENTER

Creating a Graph of Experimental Data

Graph the results of an experiment and examine the trends.

(Example: examined data relating to water vapour pressure and temperature.)

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Enter statistical data using statistics feature before executing program.

Graph plotted using automatic scaling.

Counter

Data as coordinates (starting point and finishing point).

Line drawn between set coordinates.

Whether or not lines of no. of data drawn judged.
Repeated until lines drawn by the no. of data.

PROGRAMME LIST(STAT MODE)

Title : XY GRAPH

ClrG

Rem DRAWING SD

2 .Stats L1,L2

Rem RANGE

xmin⇒Xmin

xmax⇒Xmax

ymin⇒Ymin

ymax⇒Ymax

(Xmax-Xmin) / 10⇒Xscl

(Ymax-Ymin) / 10⇒Yscl

Rem BROKEN LINE

0⇒I

Label DRAWLOOP

I+1⇒I

L1(I)⇒X

L2(I)⇒Y

L1(I+1)⇒Z

L2(I+1)⇒W

Line(X,Y,Z,W)

If (I+1) <n Goto DRAWLOOP

Wait

End

PARAMETERS

Name of parameter	Content	Name of parameter	Content
I	counter	Y	y of line starting point
X	x of line starting point	W	y of line finishing point
Z	x of line finishing point		

*n = number of statistical data

Exercise

The following table shows examined water vapour pressure. Draw a graph of this data.

Temperature [°C]	0	10	20	30	40	50	60	70	80	90	100
Pressure [mmHg]	4.581	9.205	17.532	31.826	55.339	92.558	149.47	223.79	355.29	525.90	760.00

Set up condition: decimal point in Float Pt Mode.

2nd F SET UP C * 1 * CL

Step

- 1** Enter statistical data into L1 and L2.

Key Operation

STAT A * ENTER

Display

(When using EL-9650)

No	1: L1	2: L2	3: L3
1	4.581		
2	9.205		
3	17.532		
4	31.826		
5	55.339		
6	92.558		

2

**0 ENTER 1 0 ...
1 0 0 ENTER**

(Other numbers not shown)

No	1: L1	2: L2	3: L3
1	0	4.581	
2	10	9.205	
3	20	17.532	
4	30	31.826	
5	40	55.339	
6	50	92.558	

3

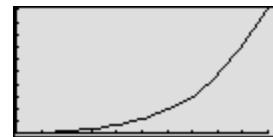
**4 • 5 8 1 ENTER
... 7 6 0 ENTER**

No	1: L1	2: L2	3: L3
7	60	149.47	
8	70	223.79	
9	80	355.29	
10	90	525.9	
11	100	760	
12			

4

- Specify the programme mode.
Select the title XY GRAPH.

(Drawing of graph)



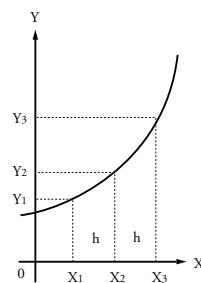
Ordinary Differential Equations

Enter the initial conditions (X, Y) with the step H and interval T. Use Runge Kutta Gill method to solve the ordinary differential equation of first order.

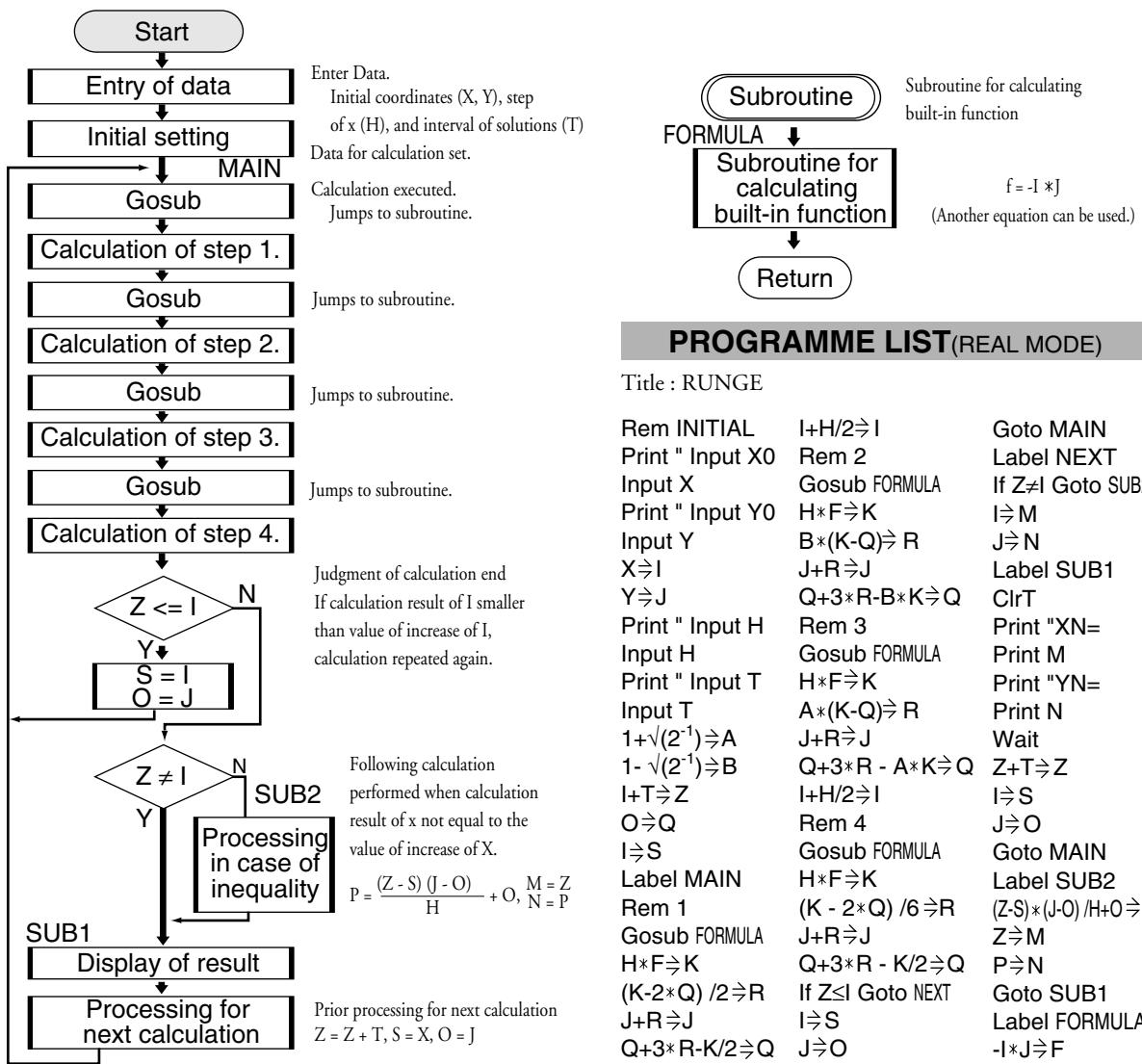
Calculation

Use the following four steps of Runge Kutta Gill method to find the equation X_{n+1} and Y_{n+1} from X_n and Y_n . Input $Q_0 = 0$ at the starting point X_0 .

1. $K_0 = Hf(X_n, Y_n)$, $R_1 = (1/2)(K_0 - 2Q_0)$, $Y^{(1)} = Y_n + R_1$
2. $Q_1 = Q_0 + 3R_1 - (1/2)K_0$
 $K_1 = Hf(X_n + H/2, Y^{(1)})$, $R_2 = (1 - \sqrt{1/2})(K_1 - Q_1)$, $Y^{(2)} = Y^{(1)} + R_2$
3. $Q_2 = Q_1 + 3R_2 - (1 - \sqrt{1/2})K_1$
 $K_2 = Hf(X_n + H/2, Y^{(2)})$, $R_3 = (1 + \sqrt{1/2})(K_2 - Q_2)$, $Y^{(3)} = Y^{(2)} + R_3$
4. $Q_3 = Q_2 + 3R_3 - (1 + \sqrt{1/2})K_2$
 $K_3 = Hf(X_{n+1}, Y^{(3)})$, $R_4 = (1/6)(K_3 - 2Q_3)$, $Y_{n+1} = Y^{(3)} + R_4$
 $Q_4 = Q_3 + 3R_4 - (1/2)K_3$



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PARAMETERS

Name of parameter	Content	Name of parameter	Content
A	value of $1 + \sqrt{1/2}$	S	value of X_{n-1}
B	value of $1 - \sqrt{1/2}$	T	interval
F	$f(I, J)$	I	X_n
H	step	J	Y_n
K	calculating working area	Z	value of increase of X
O	value of Y_{n-1}	X	input of X_0
P	increase of J	Y	input of Y_0
Q	value of Q_n	M	indicates X_n
R	value of R_n	N	indicates Y_n

Exercise

Initial settings: $Y = 10$ when $X = 0$. Find J when $H = 0.01$, $T = 0.03$ and $I = 0.03, 0.06\cdots$.
(The built-in differential equation is $F = -I * J$.)

Set up condition: angle unit in Rad Mode and decimal point in Float Pt Mode.

2nd F SET UP B * 2 * C * 1 * CL

1

Specify the programme mode.
Select the title RUNGE.

2nd F PRGM A *

Display
(When using EL-9650)

RUNGE
Input X0
X=?

2

Enter the values of X_0 , Y_0 , H and T.

0 ENTER 1 0 ENTER

0 • 0 1 ENTER

0 • 0 3 ENTER

RUNGE
Input X0
X= 0
Input Y0
Y= 10
Input H
H= 0.01
Input T
T= 0.03

3

(Display of X_1)
(Display of Y_1)

ENTER

**XN= .03
YN= 9.995501012**

4

(Display of X_2)
(Display of Y_2)

ENTER

**XN= .06
YN= 9.98201619**

5

(Display of X_3)
(Display of Y_3)

ENTER

**XN= .09
YN= 9.959581902**

Similar operation is performed hereafter.

Analysing with One-way Layout Method

Use the one-way layout method to verify whether there is a relation to the results achieved based on one condition. Analysis of variance is carried out with this method.

Calculation

Analysis of variance chart of one-way layout method

	Sum of squares (S)	Degree of freedom (θ)	Variance (V)	Variance ratio (F)
Factor	$S_A = [A] - [X]$	$\theta_A = A - 1$	$V_A = S_A \div \theta_A$	$F_A = V_A \div V_E$
Error	$S_E = [AS] - [A]$	$\theta_E = A(N-1)$	$V_E = S_E \div \theta_E$	
Total	$S_T = [AS] - [X]$	$\theta_T = AN - 1$		

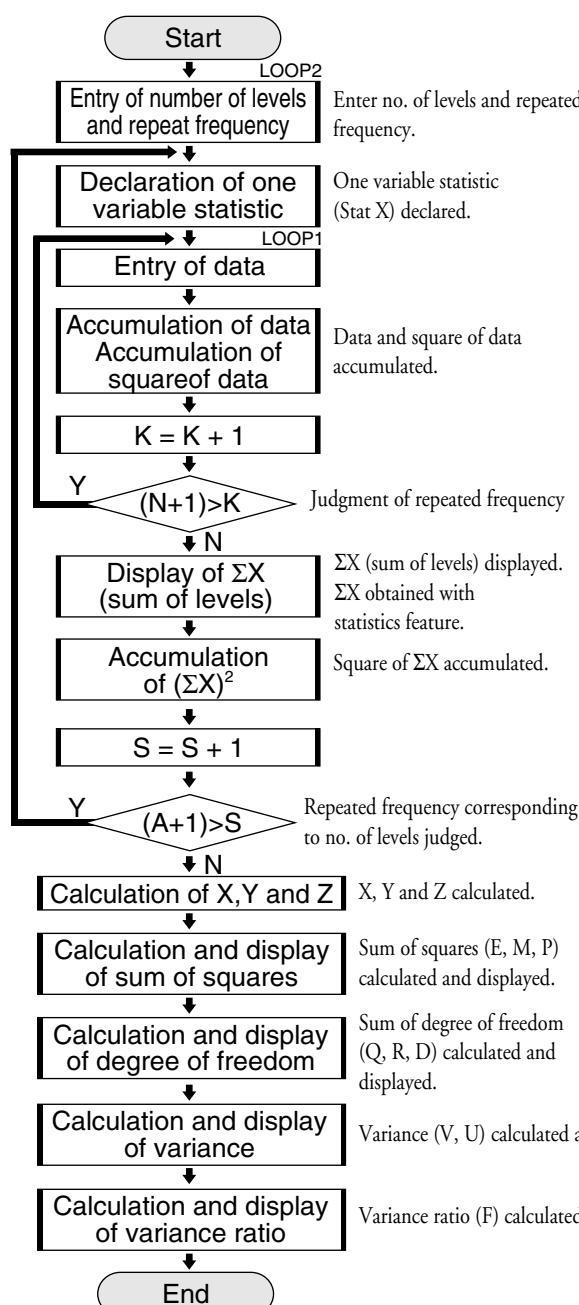
$$[X] = (\sum \sum X_{ij})^2 \div AN$$

$$[A] = \sum i (\sum j X_{ij})^2 \div N$$

$$[AS] = \sum i \sum j (X_{ij})^2$$

A : number of levels
N: repeated frequency
X : number of data

FLOWCHART



PROGRAMME LIST(STAT MODE)

Title : VARIANCE

```

Rem INPUT          W/N → Y
Print "Input LEVEL C → Z
Input L           Rem SUM OF SQUARES
L → A            Y-X → E
Print "Input TIMES Z-Y → M
Input T           Z-X → P
T → N            Print "SUM OF SQUARES
0 → W            Print E
0 → B            Print "ERROR SUM OF SQUARES
0 → C            Print M
1 → S            Wait
Label LOOP2       Print "TOTAL SUM OF SQUARES
N → dim(L1)      Print P
1 → K            Wait
Label LOOP1       Rem DEGREES OF FREEDOM
ClrT             A-1 → Q
S → L            A*(N-1) → R
K → T            A*N-1 → D
Print "Input DATA Print "DEGREES OF FREEDOM
Print "LEVEL      Print Q
Print L           Print "DEGREES OF FREEDOM _____
Print "TIME        Print R → ABOUT ERRORS
Print T           Wait
Input I           Print "SUM OF DEGREES OF FREEDOM
I → L1(K)         Print D
B+I → B          Wait
C+I² → C          Rem VARIANCE
K+1 → K          E/Q → V
If (N+1)>K Goto LOOP1 M/R → U
1_Stats L1        Print "VARIANCE
Σx → J           Print V
Print "Σx=         Print "VARIANCE OF ERRORS
Print J           Print U
Wait              Wait
W+(Σx)² → W      Rem VARIANCE RATIO
S+1 → S           V/U → F
If (A+1)>S Goto LOOP2 Print "VARIANCE RATIO
Rem CALCULATE    Print F
B²/A/N → X        End
  
```

PARAMETERS

Name of parameter	Content	Name of parameter	Content
A	number of levels	V	variance factor
I	input of data	U	variance error
K	loop 1 counter	Y	$\Sigma i (\Sigma jxij)^2 / n$
J	indicating Σx	Q	degree of freedom factor
N	repeated frequency	R	degree of freedom error
S	loop 2 counter	D	degree of freedom total
X	$(\Sigma \Sigma xi)^2 / a/n$	T	input and indicating frequency
Z	$\Sigma i \Sigma j (xij)^2$	L	input and indicating number of levels
F	variance ratio factor	W	total sum of squares of each level
E	sum of squares factor	B	total sum (all data)
M	sum of squares error	C	stotal sum of squares (all data)
P	sum of squares total		

Exercise

When a mouse is given a dosage of hormone, the relationship between dosage amount and increase of mouse weight is as shown in the following table. Find the analysis of variance. If the value of the variance ratio is larger than the value of F-distribution table of the 5% level of significance, the relationship between the hormone amount and the increase of mouse weight is a causal relation.

		Increase mouse weight (grams/day)					
			10	20	30	40	50
Hormone (grams/mouse)	10	882	891	864	888	885	
	20	923	915	923	912	930	
	30	933	939	925	940	932	

The number of levels (number of columns in the table) is A = 3

The repeated frequency (number of rows in the table) is N = 5

Set up condition: decimal point in Float Pt Mode.

2nd F SET UP C * 1 * CL

Step**Key Operation****Display**

(When using EL-9650)

- 1** Specify the programme mode.
Select the title VARIANCE.

2nd F PRGM A *

VARIANCE
Input LEVEL
L=?

- 2** Enter the number of levels and
the repeated frequency.

3 ENTER 5

VARIANCE
Input LEVEL
L=
3
Input TIMES
T=
5

- 3**

ENTER

Input DATA
LEVEL 1
TIME 1
I=?

Step**Key Operation****Display**

(When using EL-9650)

- 4** Enter the statistical data in level 1.

8 8 2 ENTER 8 9 1
 ENTER 8 6 4 ENTER
 8 8 8 ENTER 8 8 5
 ENTER

LEVEL 1
 TIME 5
 I= 885
 Σx = 4410

(Display of total of hormone 10 g)

- 5** Enter the statistical data in level 2.

ENTER 9 2 3 ENTER
 9 1 5 ENTER 9 2 3
 ENTER 9 1 2 ENTER
 9 3 0 ENTER

LEVEL 2
 TIME 5
 I= 930
 Σx = 4603

(Display of total of hormone 20 g)

- 6** Enter the statistical data in level 3.

ENTER 9 3 3 ENTER
 9 3 9 ENTER 9 2 5
 ENTER 9 4 0 ENTER
 9 3 2 ENTER

LEVEL 3
 TIME 5
 I= 932
 Σx = 4669

(Display of total of hormone 30 g)

- 7**

(Display of sum of squares)
 (Display of error sum of squares)

ENTER

I= 932
 Σx = 4669
 SUM OF SQUARES 7245.733334
 ERROR SUM OF SQUARES 802

- 8**

(Display of sum of squares)

ENTER

Σx = 4669
 SUM OF SQUARES 7245.733334
 ERROR SUM OF SQUARES 802
 TOTAL SUM OF SQUARES 8047.733334

- 9**

(Display of degrees of freedom)
 (Display of degrees of freedom about errors)

ENTER

Σx = 802
 TOTAL SUM OF SQUARES 8047.733334
 DEGREES OF FREEDOM 12
 DEGREES OF FREEDOM ABOUT ERRORS 12

- 10**

(Display of sum of degrees of freedom)

ENTER

DEGREES OF FREEDOM 2
 DEGREES OF FREEDOM ABOUT ERRORS 12
 SUM OF DEGREES OF FREEDOM 14

- 11**

(Display of variance)
 (Display of variance of errors)

ENTER

Σx = 12
 SUM OF DEGREES OF FREEDOM 14
 VARIANCE 3622.866667
 VARIANCE OF ERRORS 66.83333333

- 12**

(Display of variance ratio)

ENTER

VARIANCE 14
 VARIANCE OF ERRORS 66.83333333
 VARIANCE RATIO 54.2074813

The F-distribution chart shows that the value of F of upper probability P = 5% is 3.98. Since f > 3.98 in this example, the relationship between the hormone amount and the increase of mouse weight is a causal relation with 5% level of significance.

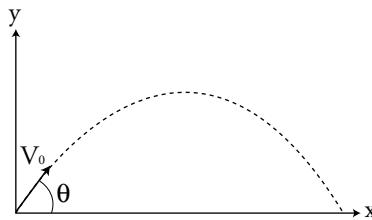
Calculating Parabolic Motion

Display on a graph the altitude change and the horizontal distance over a period of time when an object is thrown at initial velocity V_0 and angle θ , and find the horizontal distance and altitude after t seconds. Specify the angle in Deg.

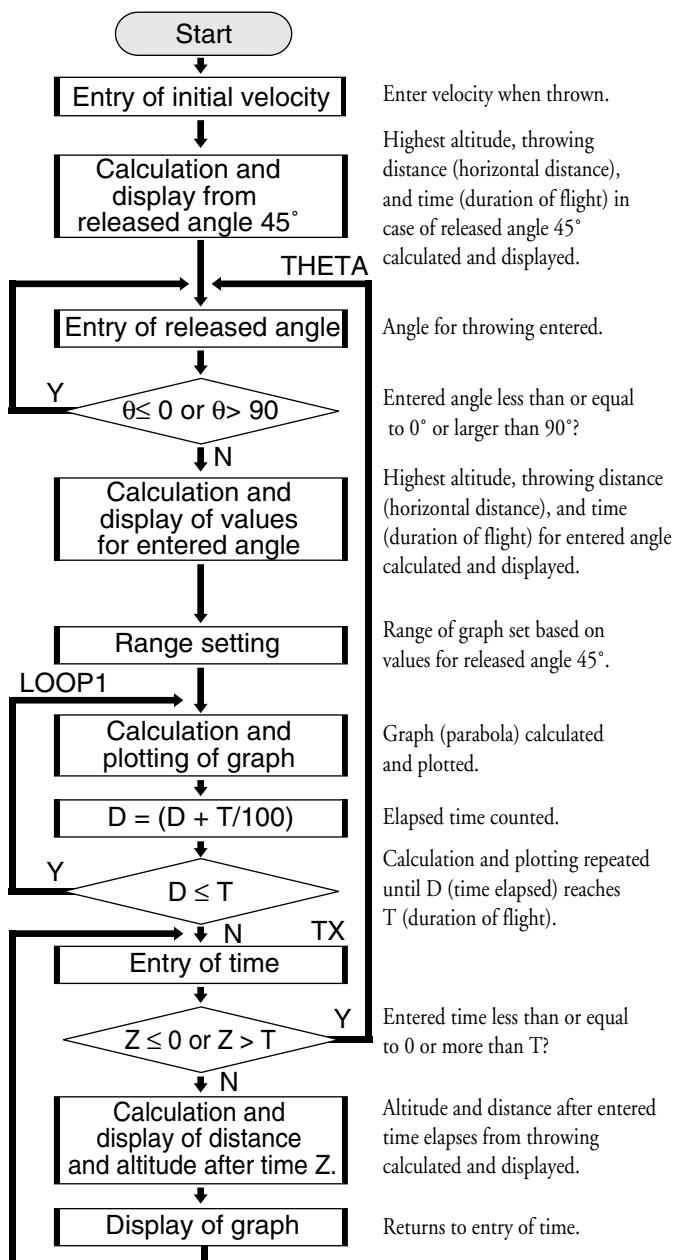
Calculation

$$X = V_0 \cdot \cos \theta \cdot T \quad Y = V_0 \cdot \sin \theta \cdot T - \frac{1}{2} g T^2$$

Initial velocity V_0 [m/s]
 Angle θ [°]
 Gravitational acceleration $g = 9.8$ [m/s²]
 Time T [s]



FLOWCHART



PROGRAMME LIST(REAL MODE)

```

Title : PARABOLA
Print "V0 (M/S),θ,T(S)      0⇒Xmin
Print "Input V0            0⇒Ymin
Input V                  B⇒Xmax
2*V*sin 45/9.8⇒A        C⇒Ymax
V^2/9.8⇒B
V^2/19.6⇒C
Print "HMAX=              0⇒D
Print C                  Label LOOP1
Print "LMAX=              V*cos θ*D⇒X
Print B                  V*sin θ*D-(0.5*9.8*D^2)⇒Y
Print "TMAX=              PntON(X,Y)
Print A                  D+(T/100)⇒D
If D≤T Goto LOOP1
Wait
Label TX
Label THETA
Input θ
If θ ≤ 0 Goto THETA
If θ > 90 Goto THETA
V^2*(sin θ)^2/19.6⇒H
V^2*sin (2θ)/9.8⇒L
2*V*sin θ/9.8⇒T
Print "X=
Print H
Print "L=
Print L
Print "T=
Print T
Wait
C/10 ⇒Yscl
B/10 ⇒Xscl
Line(0,Y,X,Y)
Line(X,0,X,Y)
Wait
Goto TX
0000
  
```

PARAMETERS

Name of parameter	Content	Name of parameter	Content
H	highest altitude	Xscl	scale of x-coordinate
L	horizontal distance	Z	input of time period
T	time	V	initial velocity (V_0)
X	distance (after time Z)	θ	angle (released angle)
Y	altitude (after time Z)	C	highest altitude when released at 90°
D	time elapsed	B	horizontal distance when released at 45°
Yscl	scale of y-coordinate	A	time period when released at 45°

Exercise

Find the horizontal distance and altitude three seconds after an object is thrown, when the initial velocity is 25m/sec and the angle is 52° .

Set up condition: angle unit in Deg mode, and decimal point in Float Pt mode.

2nd F SET UP B.* 1.* C.* 1.* CL

Step
1 Specify the programme mode.
Select the title PARABOLA.

2nd F PRGM A.*

Display
(When using EL-9650)

PARABOLA
 V_0 (M/S), θ , T(S)
Input V_0
 $V=?$

2 Enter the value of the initial velocity. **2 5 ENTER**

(Highest altitude when released at 90°)
(Distance when released at 45°)
(Time when released at 45°)

ENTER

V=
25
HMAX= 31.8877551
LMAX= 63.7755102
TMAX= 3.607687659

4 Enter the angle value. **5 2 ENTER**

(Display of highest altitude)
(Display of horizontal distance)
(Display of time until dropping of object)

ENTER

B=
52
H= 19.80105063
L= 61.88110499
T= 4.020463029

5 (Display of graph of parabola)

6 **ENTER**

H= 19.80105063
L= 61.88110499
T= 4.020463029
Input TX
 $Z=?$

7 Enter the value of time period Z. **3 ENTER**

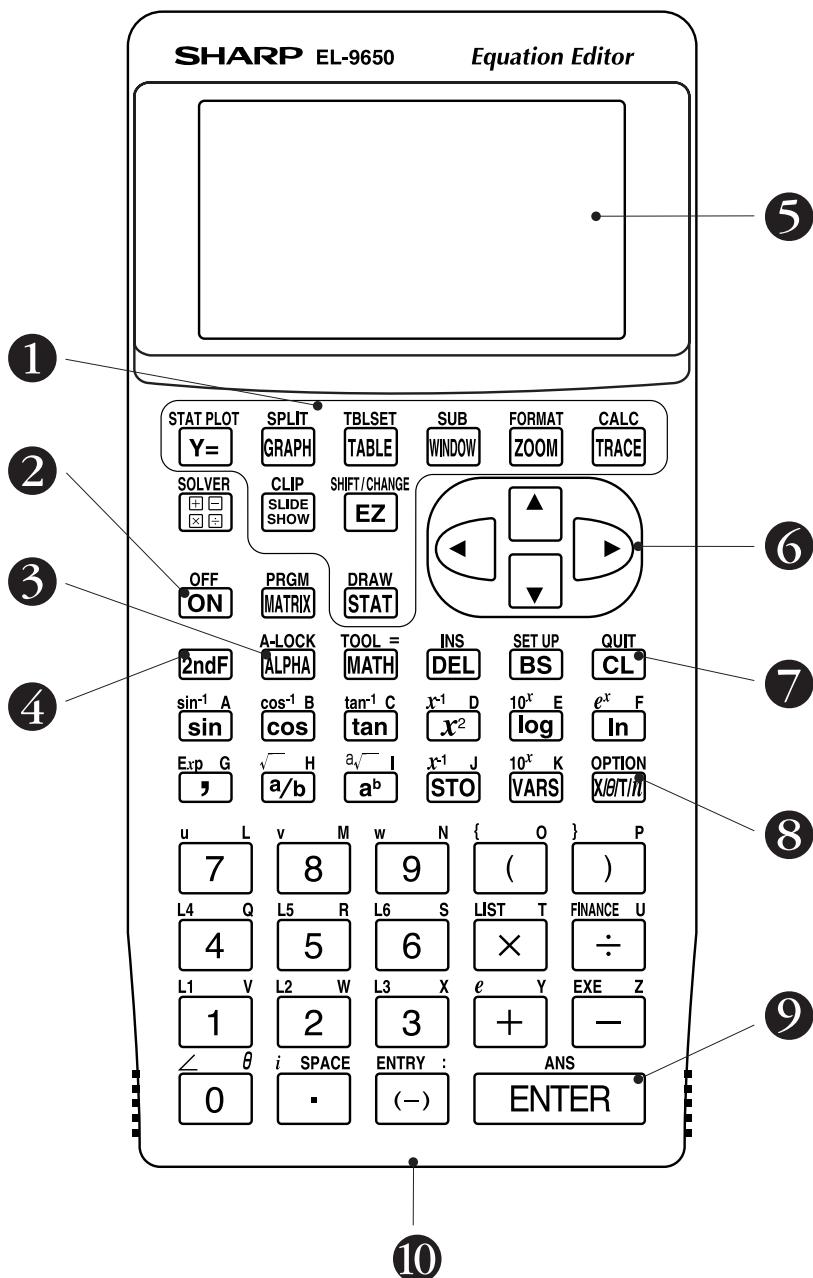
(Display of distance after Z seconds)
(Display of altitude after Z seconds)

ENTER

Input TX 4.020463029
Z= 3
X= 46.17461065
Y= 15.00080652

8 Altitude and distance after Z seconds are displayed on the parabola graph.)

Key pad for the SHARP EL-9650 Calculator



① Graphing keys

② Power supply ON/OFF key

③ Alphabet specification key

④ Secondary function specification key

⑤ Display screen

⑥ Cursor movement keys

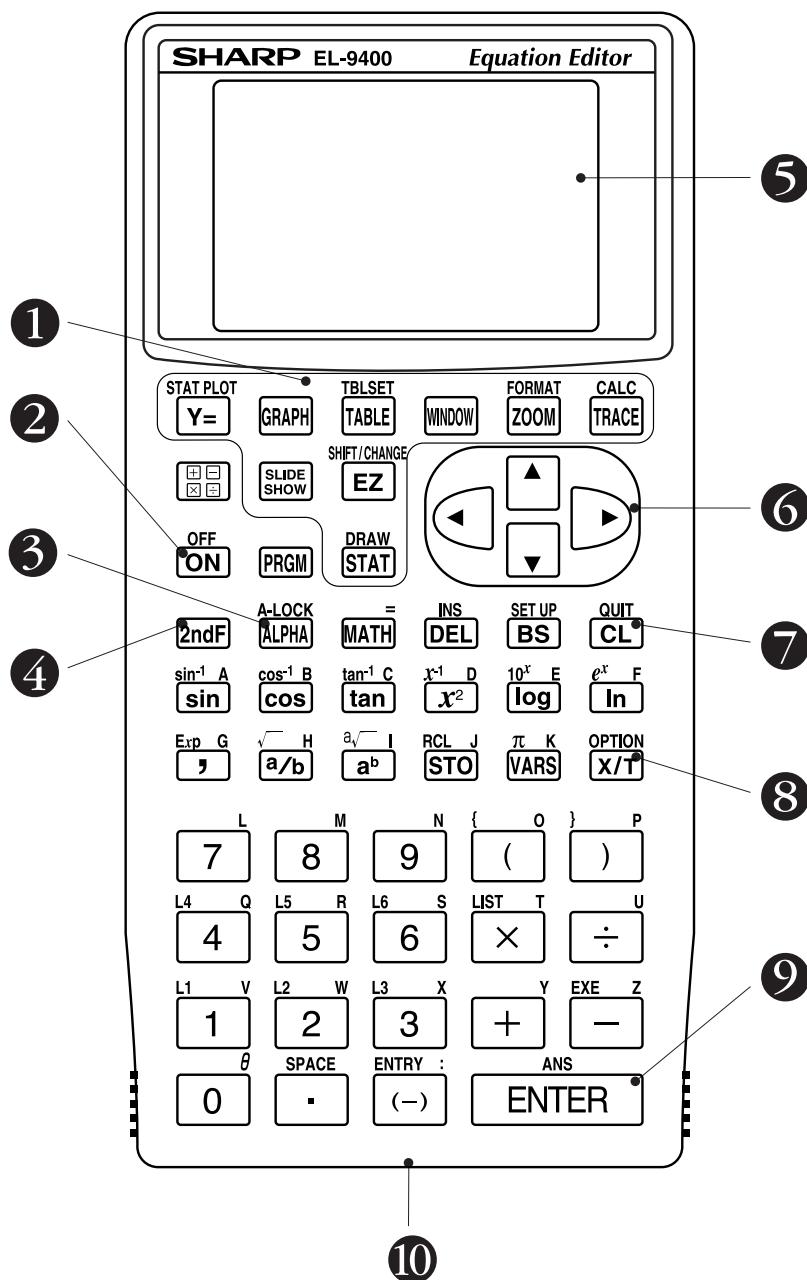
⑦ Clear/Quit key

⑧ Variable enter key

⑨ Calculation execute key

⑩ Communication port for peripheral devices

Key pad for the SHARP EL-9400 Calculator



① Graphing keys

② Power supply ON/OFF key

③ Alphabet specification key

④ Secondary function specification key

⑤ Display screen

⑥ Cursor movement keys

⑦ Clear/Quit key

⑧ Variable enter key

⑨ Calculation execute key

⑩ Communication port for peripheral devices

SHARP

Use this form to send us your contribution

Dear Sir/Madam

We would like to take this opportunity to invite you to create a mathematical problem which can be solved with the SHARP EL-9650 and 9400 graphing calculator, including the necessary procedures and definitions as outlined in the form below.

For this purpose, we would be grateful if you could complete the form and return it to us by fax or mail, specifying whether you have created the problem for the EL-9650 or the EL-9400. If your contribution is chosen, your name will be included in the next edition of The EL-9650/9400 Graphing Calculator Handbook or on our homepage. We regret that we are unable to return contributions. Also, please note that the problems you send us might be opened to the public at Sharp's home page.

We thank you for your cooperation in this project.

Name: (<input type="checkbox"/> Mr. <input type="checkbox"/> Ms.)	
School/College/Univ.: _____	
Address: _____	
Post Code:	Country:
Phone: _____	Fax: _____
E-mail: _____	

* You are making this sheet for the (EL-9650, EL-9400).

SUBJECT: Write either a title or about the subject matter.

.....

INTRODUCTION and CALCULATION:

Write a brief explanation of the subject, and the formula with definitions, including a diagram if relevant.

.....



PARAMETERS:

Define the parameters used in the programme.

PROGRAMME LIST:

List the procedure of data to be entered.

EXERCISE and SET UP CONDITION:

Include an example of a problem which can be solved with the formula. Write a step-by-step guide to solving the problem with an explanation. Detail any important conditions to be set up before solving the problem.

SHARP
SHARP CORPORATION Osaka, Japan
Fax:

SHARP Graphing Calculator



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SHARP CORPORATION OSAKA,JAPAN